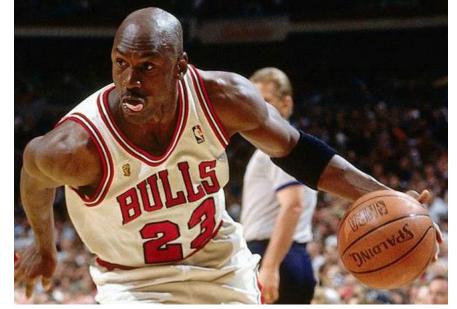
Percentiles & Z-Scores

- Lesson 2.1 -









Paul Vathis, AP Images

Wilt - 1960's

Jordan - 1990's

LeBron - 2010's





Paul Va

Today's Key Analysis Who was the G.O.A.T at scoring?



י - 2010's

Skew The Script

Lesson 2.1 Guided Notes

Handout: skewthescript.org/2-1



Topics

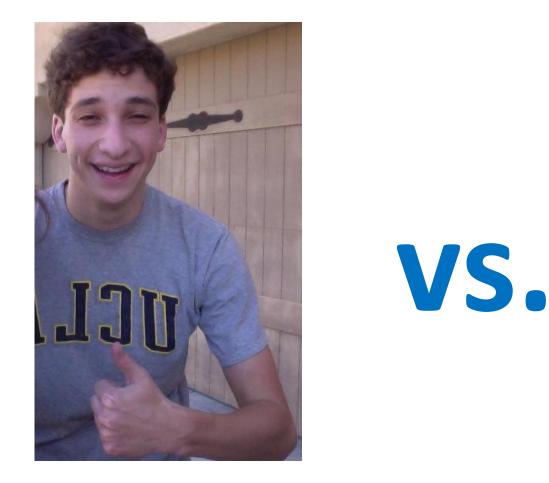
- 1. Percentiles
- 2. Cumulative Relative Frequency
- 3. Standardized Scores (Z-Scores)



Topics

- **1. Percentiles**
- 2. Cumulative Relative Frequency
- 3. Standardized Scores (Z-Scores)







Mr. Young-Saver Statistician, Math Teacher Guy Fieri Chef, Mayor of Flavortown

Skew The Script





Mr. Young-Saver Statistician, Math Teacher



They don't offer the SAT in Flavortown, USA!



Guy Fieri Chef, Mayor of Flavortown

Skew The Script

They don't offer the SAT in Flavortown, USA!

Mr. Fieri took the ACT



Guy Fieri Chef, Mayor of Flavortown

Skew The Script





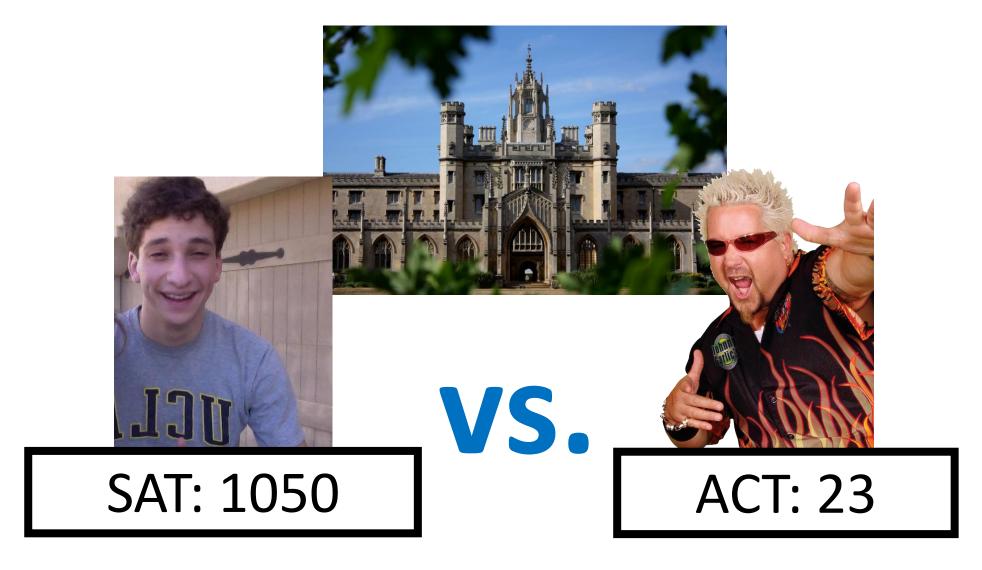


Guy Fieri Chef, Mayor of Flavortown

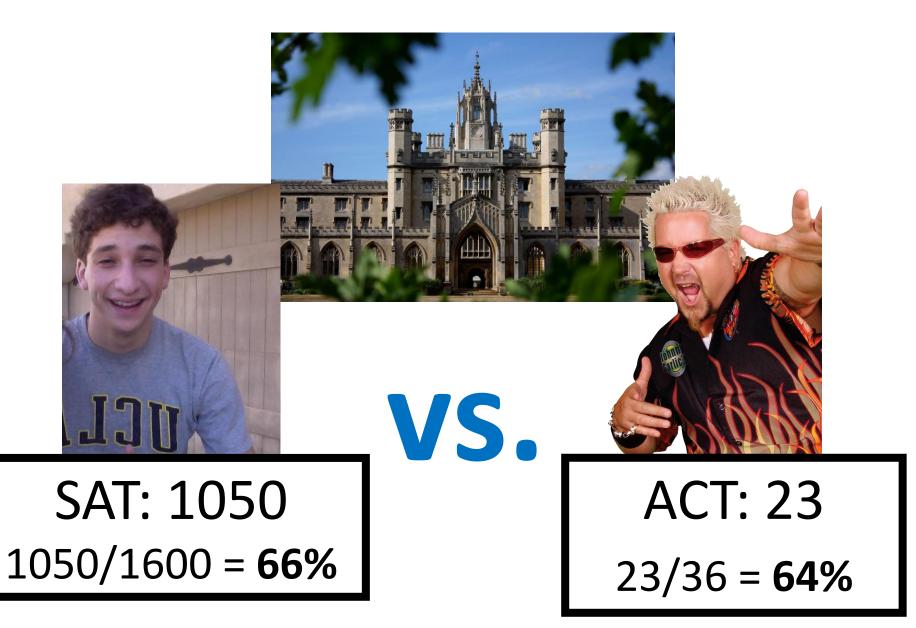
Skew The Script



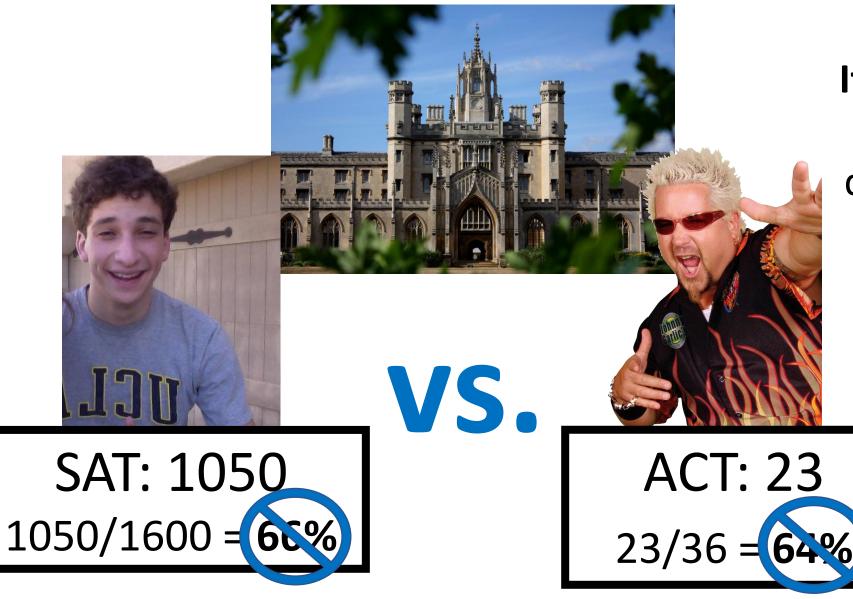




Skew The Script

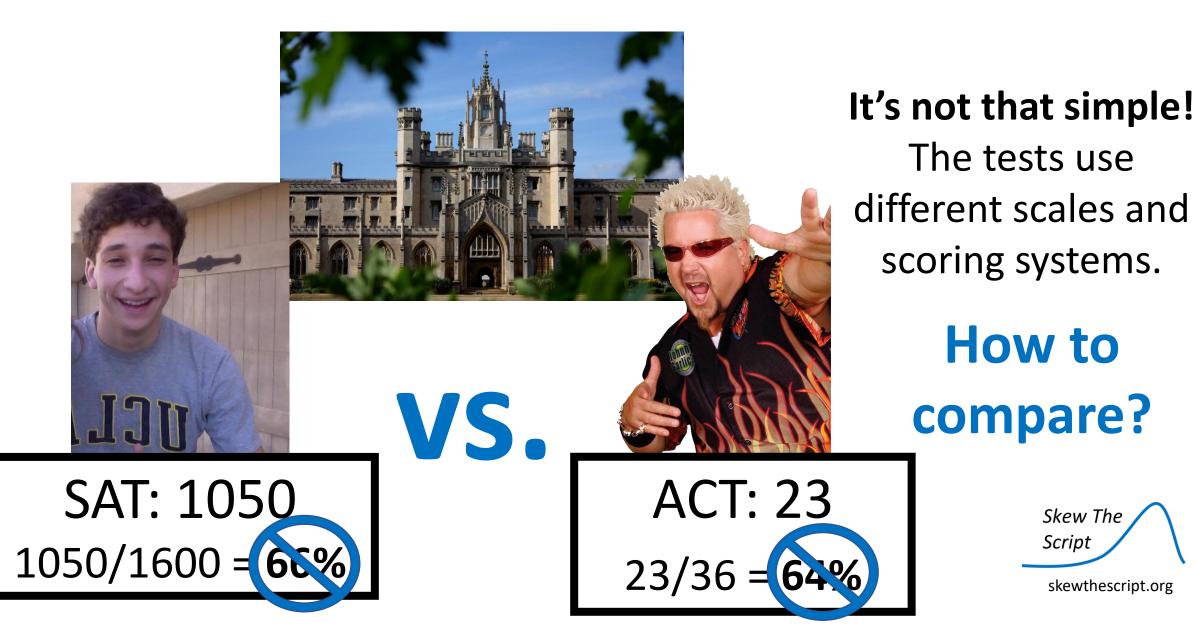


Skew The Script



It's not that simple! The tests use different scales and scoring systems.

Skew The Script



<u>Percentile</u>: the percent of data less than or equal to a certain data value.



<u>Percentile</u>: the percent of data less than or equal to a certain data value.

Note: Sometimes it's just "less than," but in AP Stats it's "less than or equal to"



<u>Percentile</u>: the percent of data less than or equal to a certain data value.

Salaries at a company (thousands of \$)

29, 32, 34, 34, 34, 34, 35, 35, 39, 43, 67, 185



<u>Percentile</u>: the percent of data less than or equal to a certain data value.

Question: At what percentile is the person who makes a salary of \$43,000?

29, 32, 34, 34, 34, 34, 35, 35, 39, 43, 67, 185



<u>Percentile</u>: the percent of data less than or equal to a certain data value.

Question: At what percentile is the person who makes a salary of \$43,000?

29, 32, 34, 34, 34, 34, 35, 35, 39, 43, 67, 185

"less than or equal to"



<u>Percentile</u>: the percent of data less than or equal to a certain data value.

Question: At what percentile is the person who makes a salary of \$43,000?

29, 32, 34, 34, 34, 34, 35, 35, 39, 43, 67, 185

10 salaries at or below \$43,000



<u>Percentile</u>: the percent of data less than or equal to a certain data value.

Question: At what percentile is the person who makes a salary of \$43,000?

29, 32, 34, 34, 34, 34, 35, 35, 39, 43, 67, 185

10 / 12 ≈ 83%



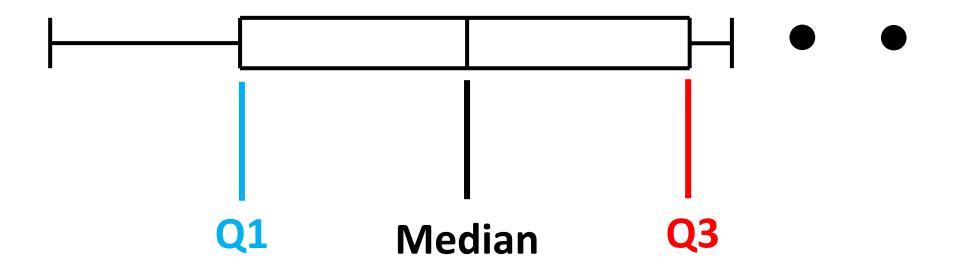
<u>Percentile</u>: the percent of data less than or equal to a certain data value.

Question: At what percentile is the person who makes a salary of \$43,000?

29, 32, 34, 34, 34, 34, 35, 35, 39, 43, 67, 185

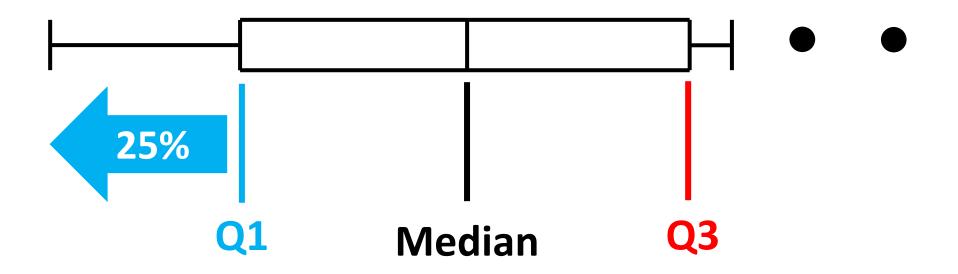
10 / 12 \approx 83% \rightarrow The salary of \$43,000 is at the 83rd percentile of salaries.





For large datasets...

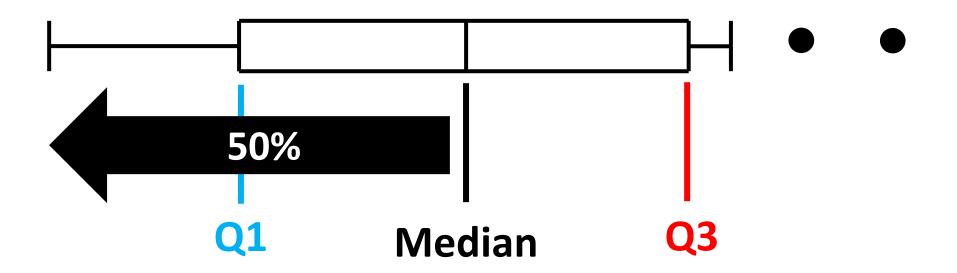




For large datasets...

Q1 is at the 25th percentile.

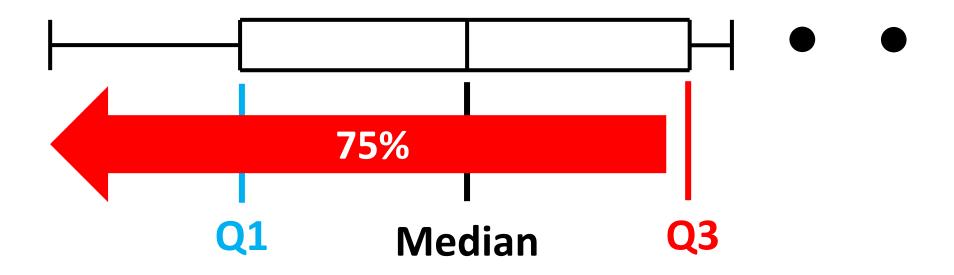




For large datasets...

The median (Q2) is at the 50th percentile.

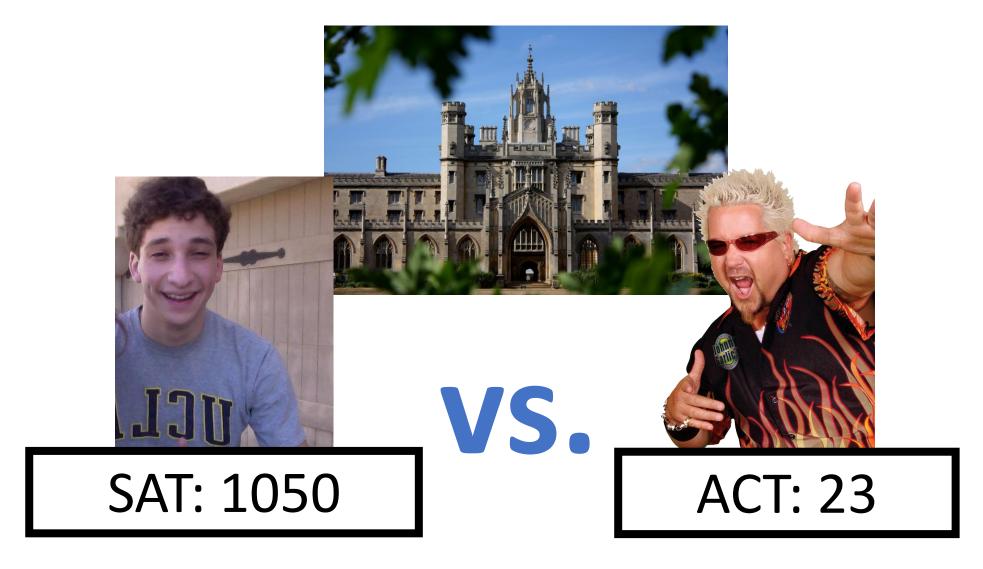
less the second set area



For large datasets...

Q3 is at the 75th percentile.

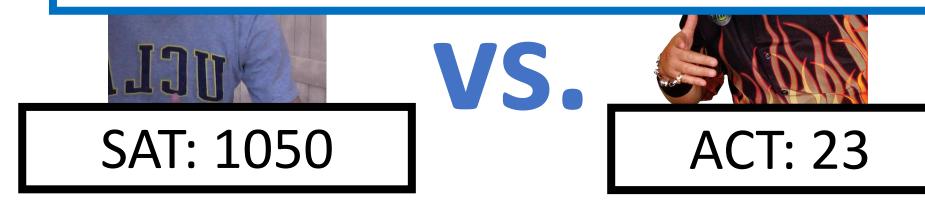




Skew The Script



What percent of people did each test-taker outscore?



Skew The Script

SAT	Percentile			
1600	100%			
1550	99.3%			
1500	98%			
1450	95%			
1400	93%			
1350	89%			
1300	84%			
1250	78%			
1200	71%			
1150	62%			
1100	53%			
1050	45%			
1000	35%			
950	26%			
900	19%			
850	13%			
800	8%			
750	5%			
700	3%			
650	2%			
600	1%			

ACT	Percentile
36	100%
35	99.9%
34	99.0%
33	98%
32	97%
31	95%
30	93%
29	91%
28	88%
27	85%
26	82%
25	78%
24	74%
23	69%
22	64%
21	58%
20	52%
19	46%
18	40%
17	33%
16	27%
15	20%
14	14%
13	9%
12	4%
11	1%
10	1%

Skew The Script

skewthescript.org

From 2019-2020 school year test reports

JJU	

SAT	Percentile
1600	100%
1550	99.3%
1500	98%
1450	95%
1400	93%
1350	89%
1300	84%
1250	78%
1200	71%
1150	62%
1100	53%
1050	45%
1000	35%
950	26%
900	19%
850	13%
800	8%
750	5%
700	3%
650	2%
600	1%



ACT	Percentile
36	100%
35	99.9%
34	99.0%
33	98%
32	97%
31	95%
30	93%
29	91%
28	88%
27	85%
26	82%
25	78%
24	74%
23	69%
22	64%
21	58%
20	52%
19	46%
18	40%
17	33%
16	27%
15	20%
14	14%
13	9%
12	4%
11	1%
10	1%

Skew The Script

skewthescript.org

From 2019-2020 school year test reports

SAT 160 155 150 145 140 135 130 125 120 115 110 105 100	600 550 450 400 350 300 250 200 150 100 050 000	_	Percentile
155 150 145 140 135 130 125 120 115 110 105	550 500 450 400 350 300 250 200 150 100 050 000)	
150 145 140 135 130 125 120 115 110 105	500 450 350 300 250 200 150 100 050 000		100%
145 140 135 130 125 120 115 110 105	450 400 350 300 250 200 150 100 050 000)	99.3%
140 135 130 125 120 115 110 105	400 350 250 200 150 100 050 000)	98%
135 130 125 120 115 110 105	350 300 250 200 150 100 050 000)	95%
130 125 120 115 110 105	300 250 200 150 100 050 000)	93%
125 120 115 110 105	250 200 150 100 050 000)	89%
120 115 110 105	200 150 100 050 000)	84%
115 110 105	150 100 050 000)	78%
110 105	100 0 50 000)	71%
105	050 000)	62%
	000)	53%
100			45%
	50)	35%
950			26%



ACT Percentile 36 100% 35 99.9% 34 99.0% 33 98% 32 97% 31 95% 30 93% 91% 29 28 88% 27 85% 26 82% 25 78% 24 74% 23 **69%** \mathbf{a} G10/

Mr. Fieri tied or outscored 69% of test takers

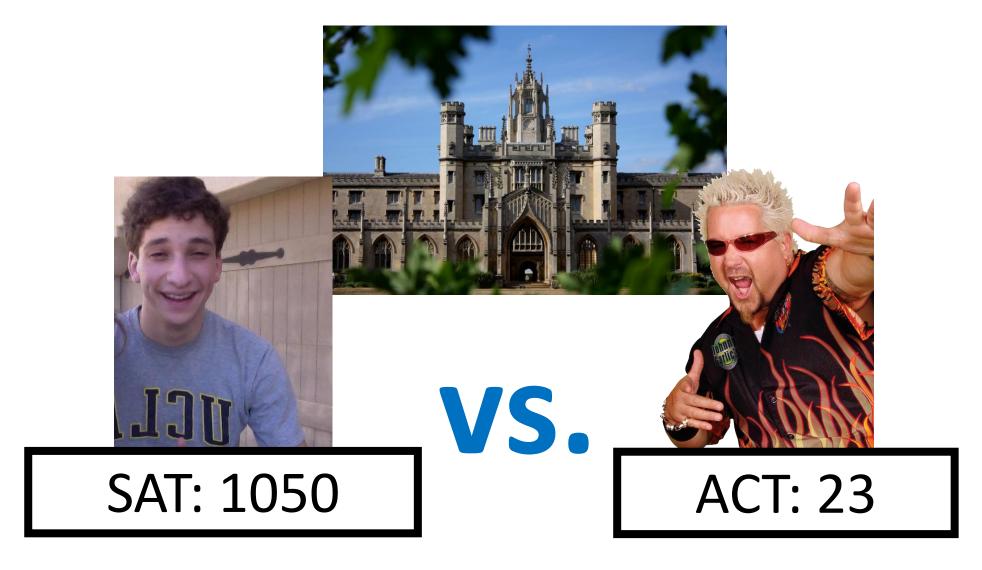
16	27%
15	20%
14	14%
13	9%
12	4%
11	1%
10	1%

Skew The Script

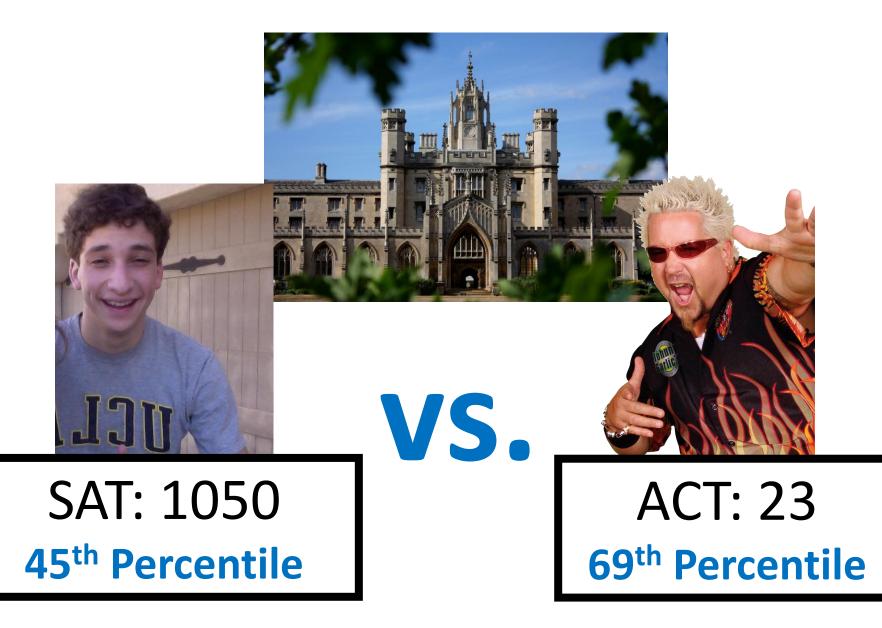
skewthescript.org

From 2019-2020 school year test reports

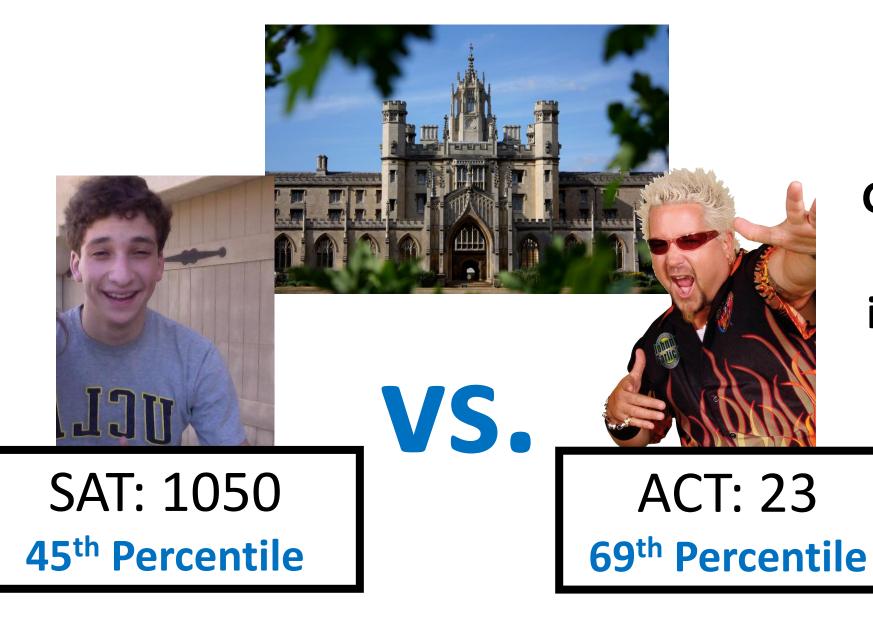
takers



Skew The Script



Skew The Script



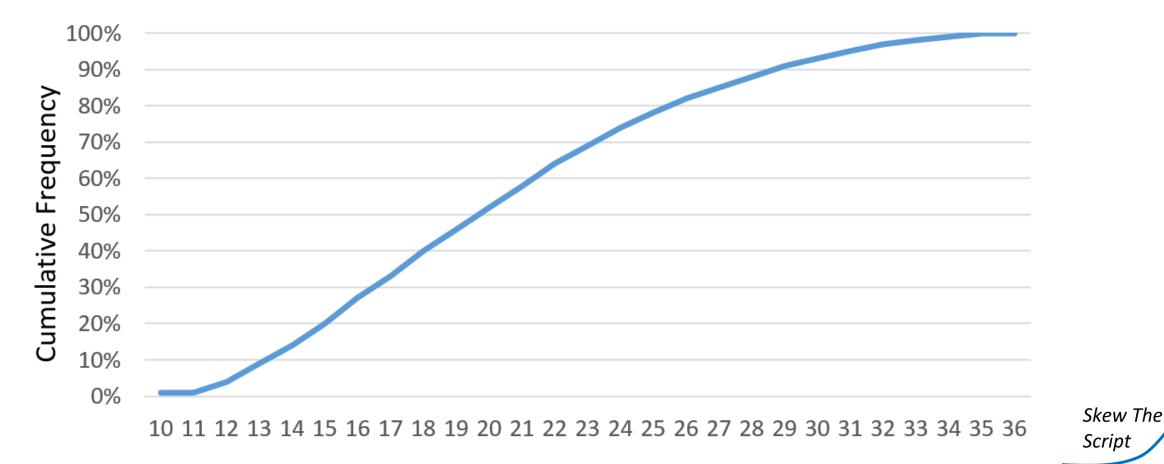
Guy Fieri's score is the more impressive one.



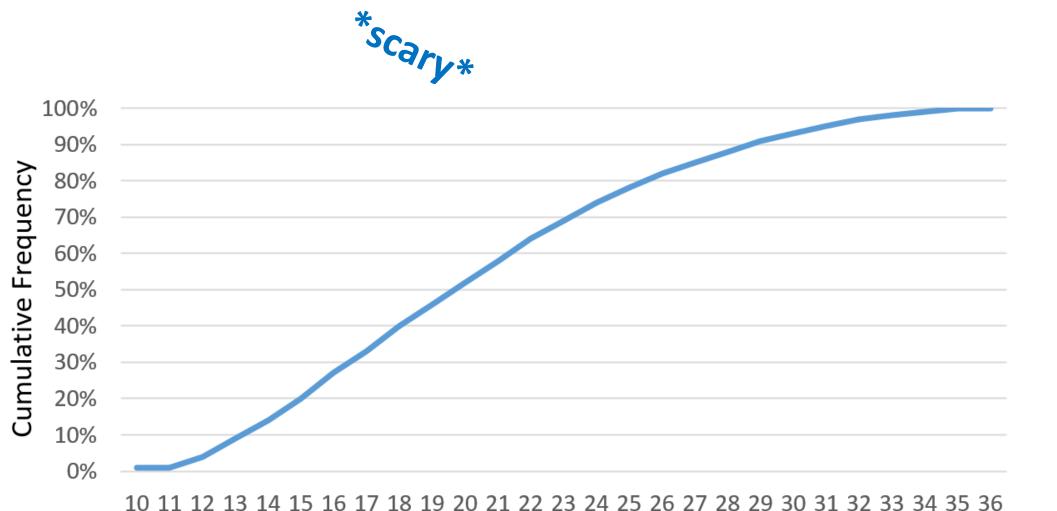
Topics

- 1. Percentiles
- 2. Cumulative Relative Frequency
- 3. Standardized Scores (Z-Scores)





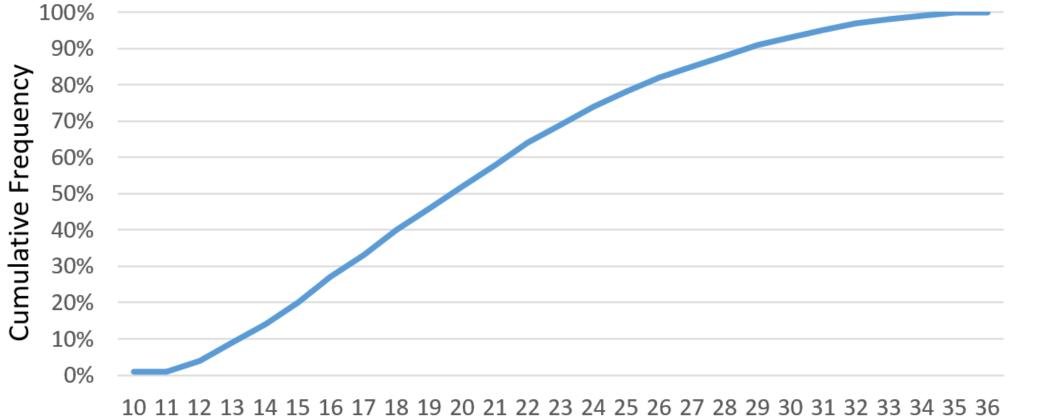
ACT Scores



Skew The Script

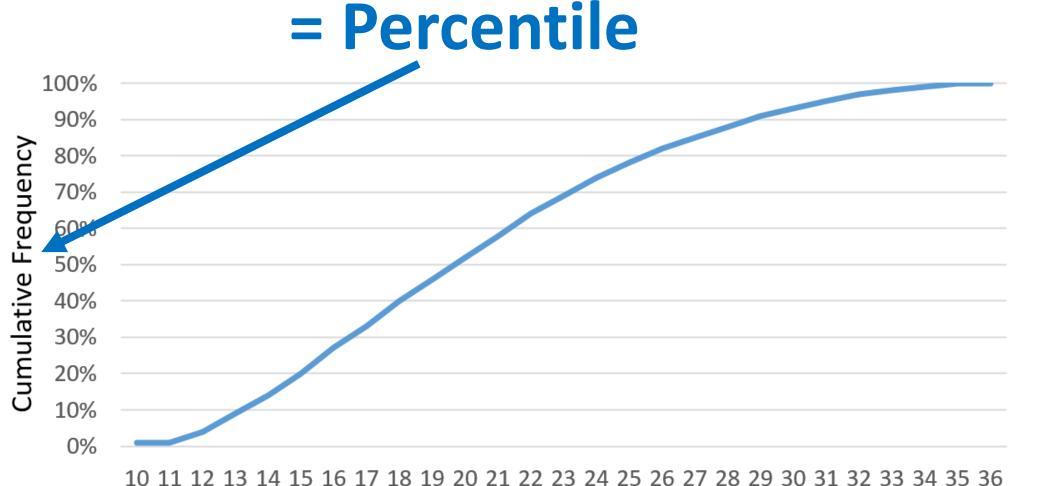
ACT Scores

Cumulative Relative Frequency Charts = Percentile



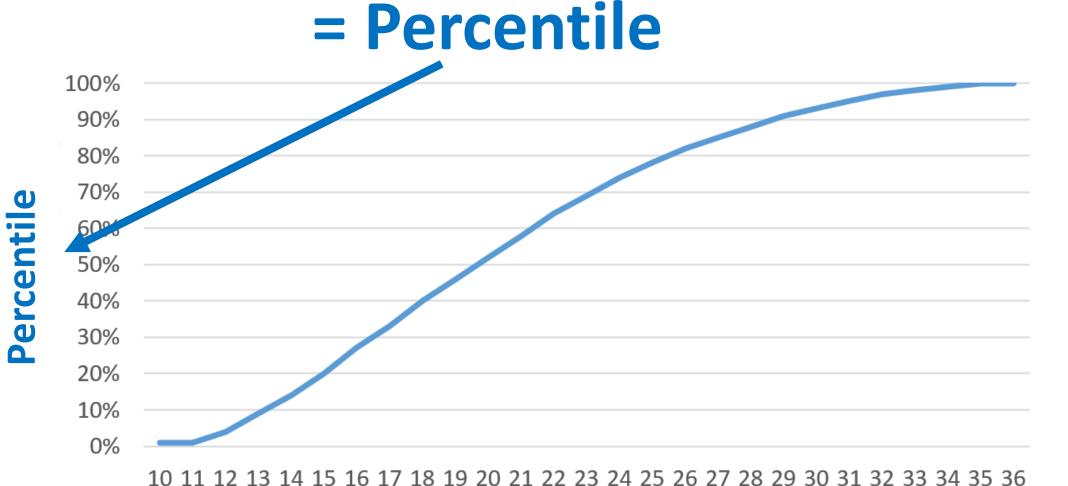
Skew The Script

ACT Scores



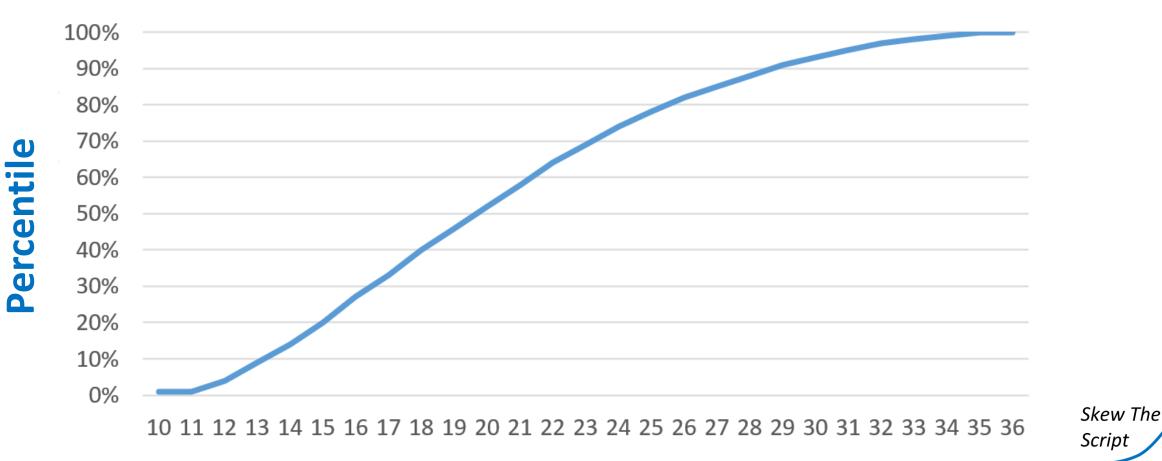
Skew The Script

ACT Scores



Skew The Script

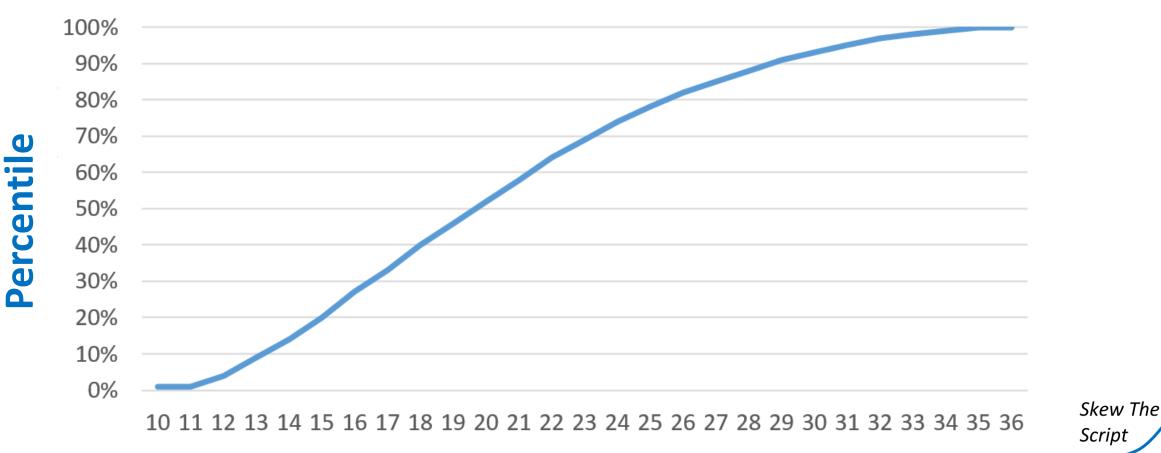
ACT Scores



skewthescript.org

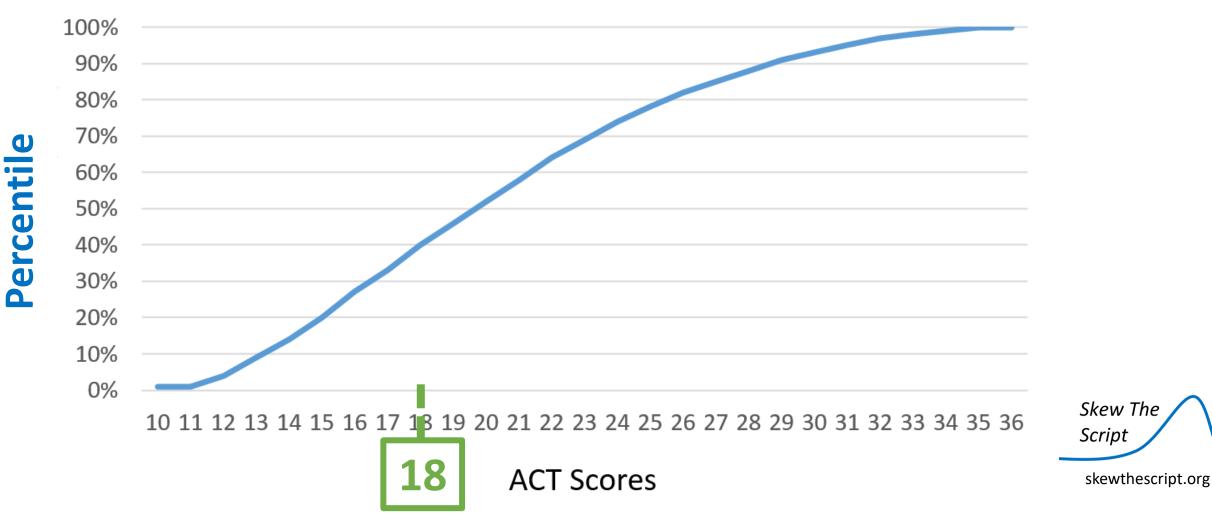
ACT Scores

Is 18 a good ACT score?

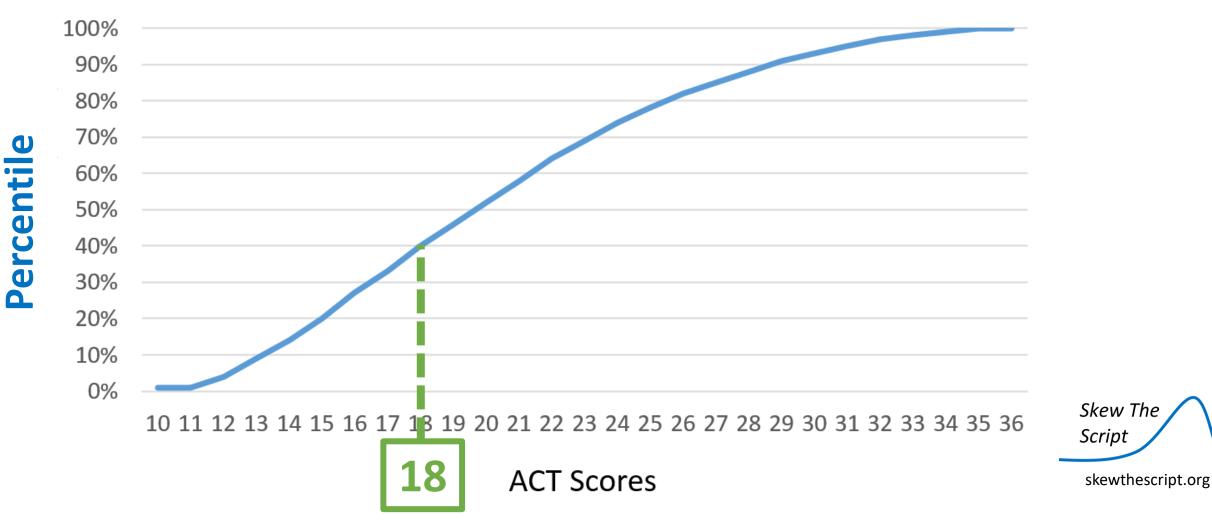


ACT Scores

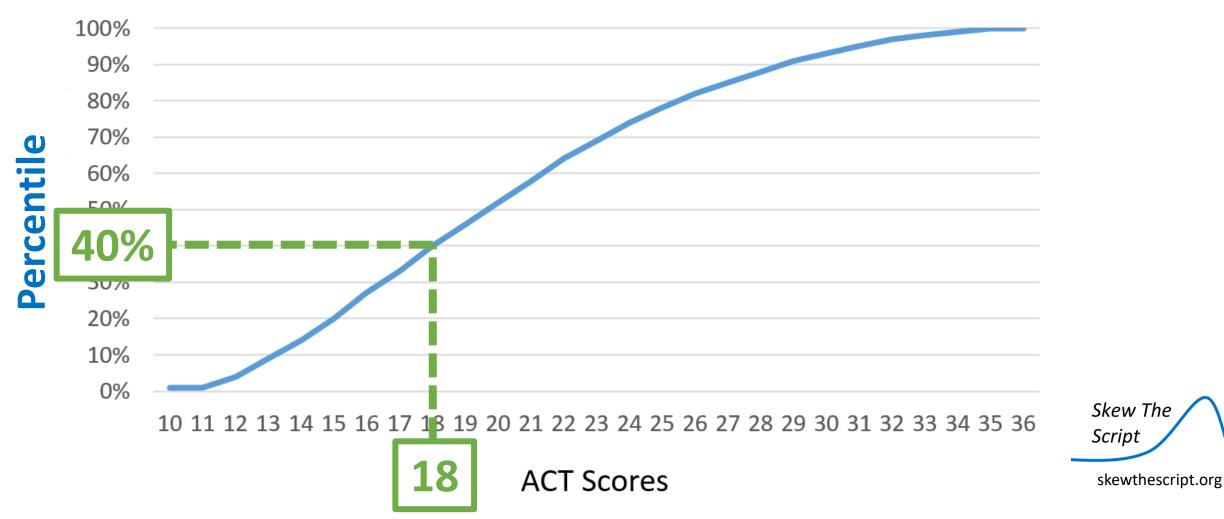
Is 18 a good ACT score?



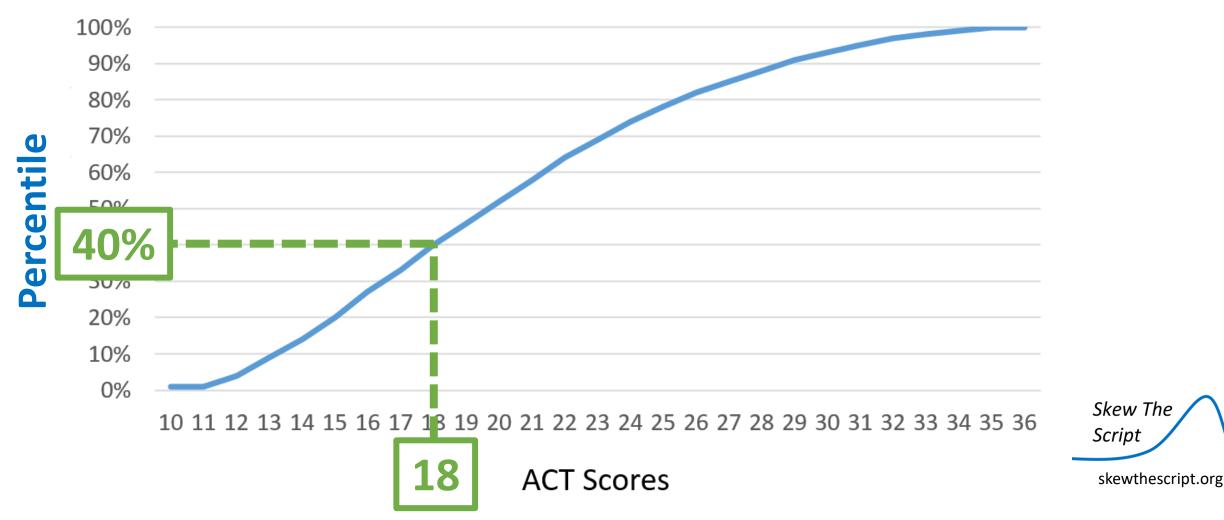
Is 18 a good ACT score?



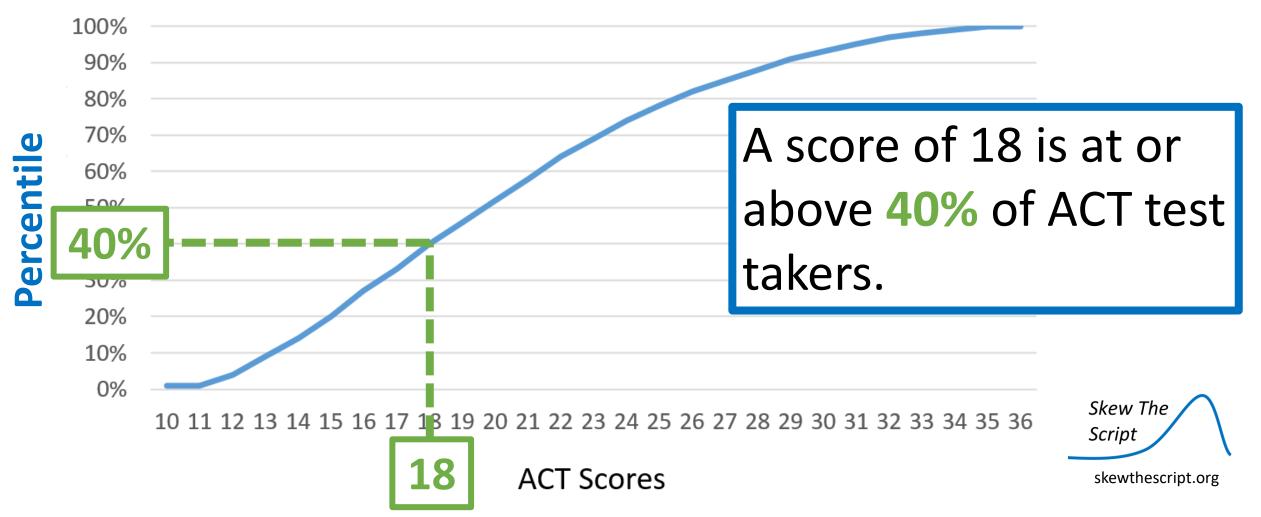
Is 18 a good ACT score?



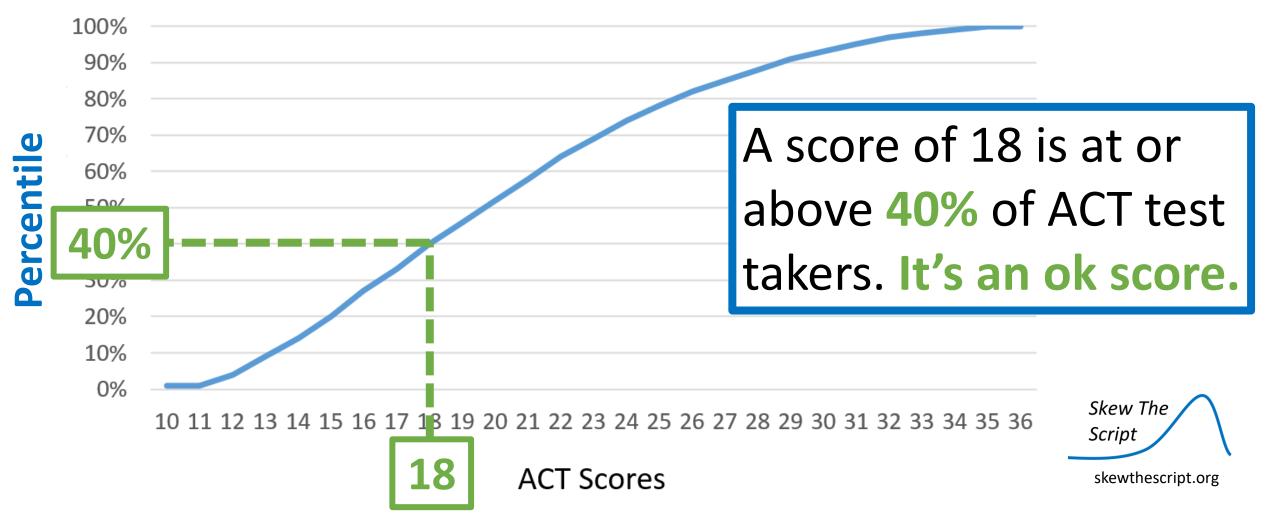
Is 18 a good ACT score? → 40th percentile



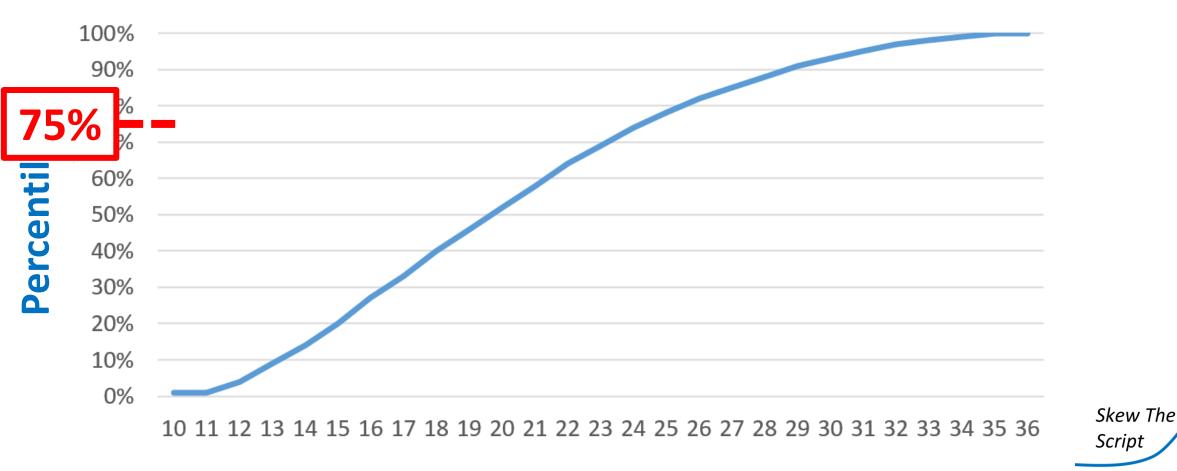
Is 18 a good ACT score? → 40th percentile



Is 18 a good ACT score? → 40th percentile

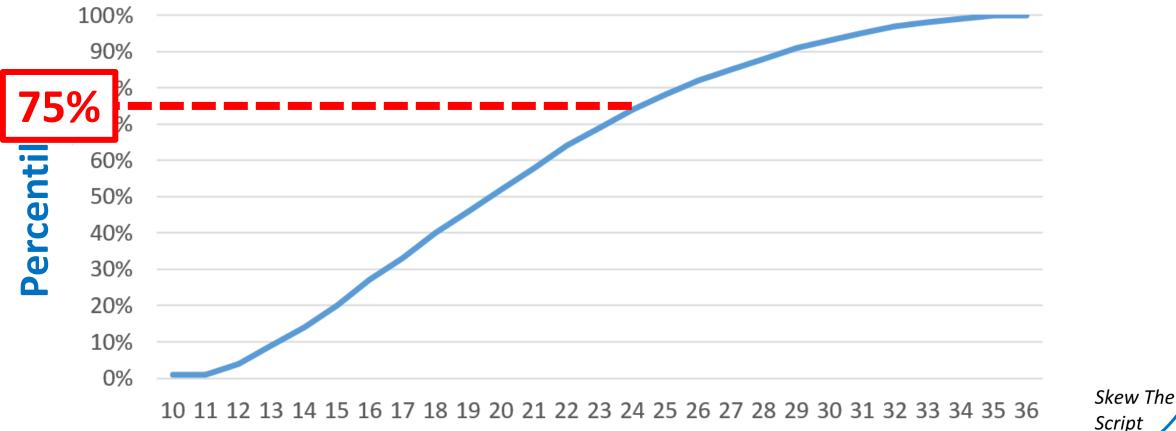


To be in the top quartile, what score do you need?



ACT Scores

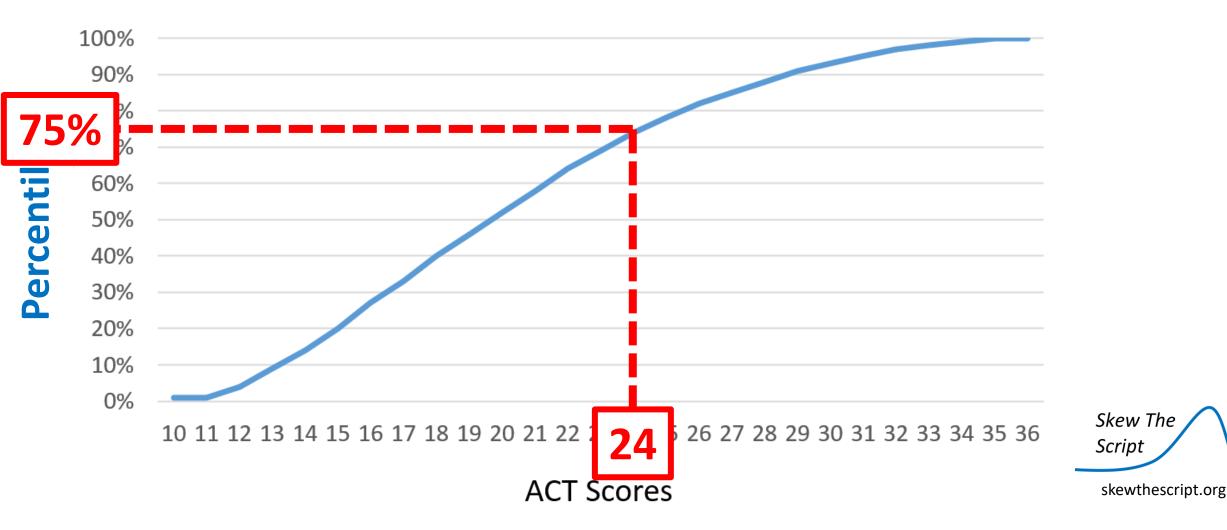
To be in the top quartile, what score do you need?



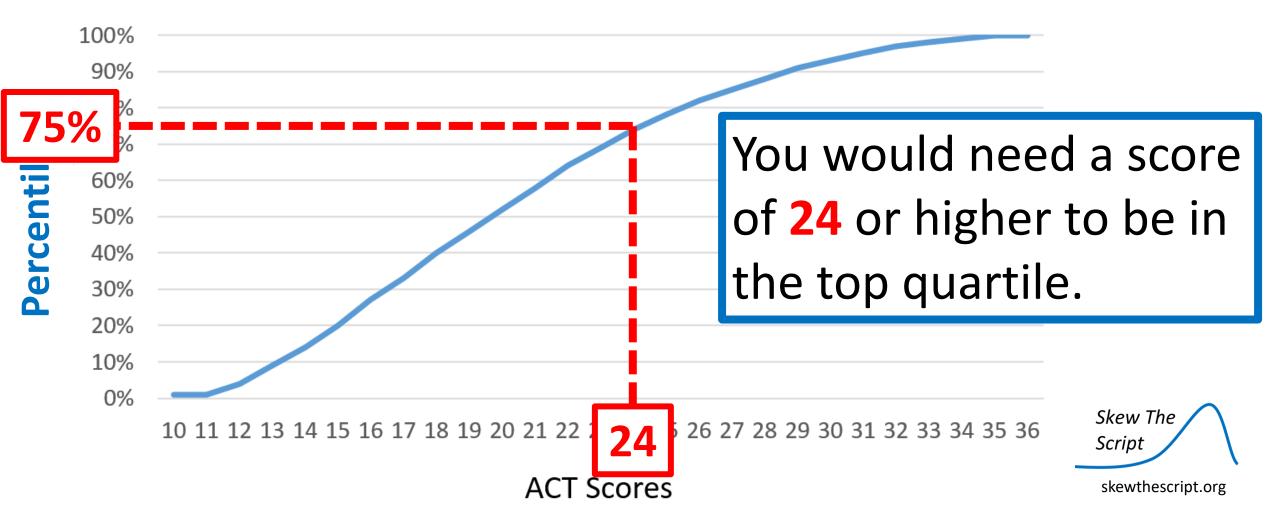
skewthescript.org

ACT Scores

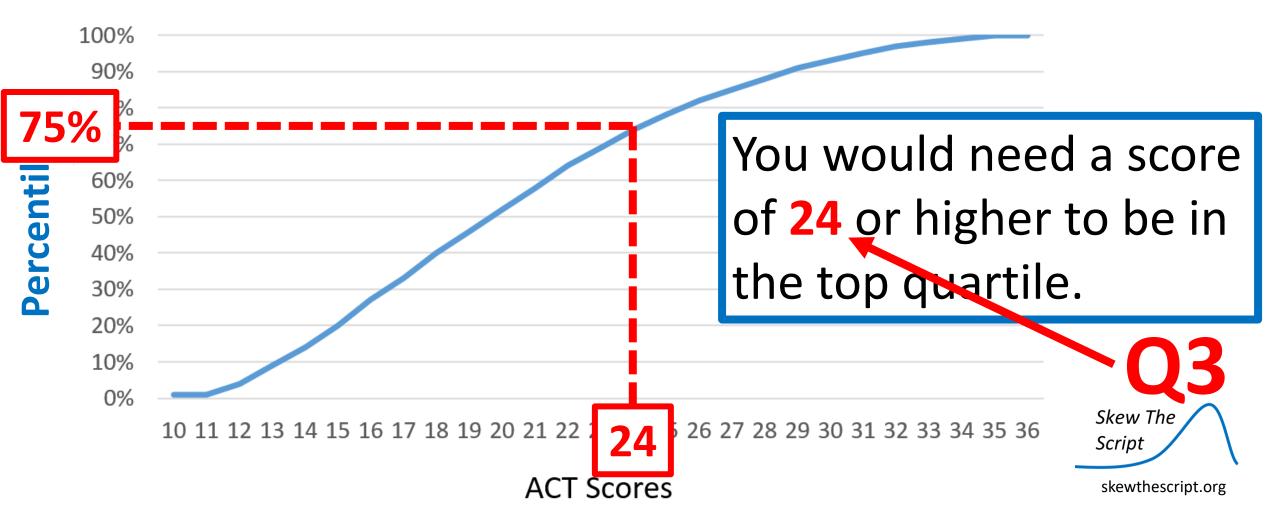
To be in the top quartile, what score do you need?



To be in the top quartile, what score do you need?



To be in the top quartile, what score do you need?



Topics

- 1. Percentiles
- 2. Cumulative Relative Frequency
- 3. Standardized Scores (Z-Scores)



Z-Scores (Standardized Score)

<u>Z-Scores</u>: measures how many standard deviations a data point is above/below the mean.



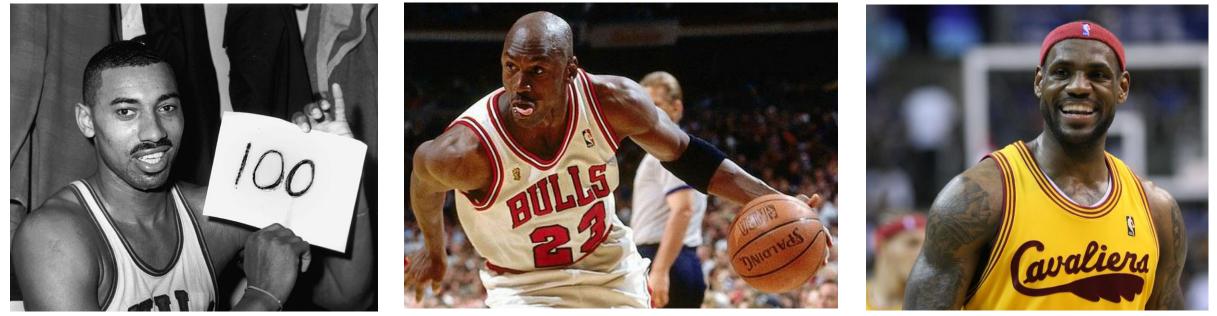
Z-Scores (Standardized Score)

<u>Z-Scores:</u> measures how many standard deviations a data point is above/below the mean.

$$z = \frac{data \ point - mean}{standard \ deviation}$$
$$z = \frac{x_i - \mu}{\sigma}$$



Who is the best **scorer**?



Paul Vathis, AP Images

Wilt - 1960's

Jordan - 1990's

LeBron - 2010's



All NBA stats used in this lesson were made possible by the data compiled in this NBA Kaggle database: kaggle.com/drgilermo/nba-players-stats

Who is the best **scorer**?



Paul Vathis, AP Images



30.1 PPG





27.1 PPG

Skew The Script

skewthescript.org

Note: All NBA data in this lesson is from 2020 and prior.

Wilt - 60's



Paul Vathis, AP Images



Jordan - 90's



LeBron - 2010's



30.1 PPG

27.1 PPG



skewthescript.org

Note: All NBA data in this lesson is from 2020 and prior

Wilt - 60's



Paul Vathis, AP Images

Jordan - 90's



LeBron - 2010's



30.1 PPG 60's NBA: $\mu = 10.8 \text{ ppg}$

30.1 PPG 90's NBA: $\mu = 8.7 \text{ ppg}$

27.1 PPG 2010's NBA: $\mu = 8.4 \text{ ppg}$



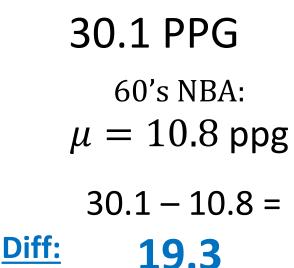
skewthescript.org

Note: All NBA data in this lesson is from 2020 and prior

Wilt - 60's



Paul Vathis, AP Images



Jordan - 90's



30.1 PPG
90's NBA: $\mu = 8.7 \text{ ppg}$
30.1 – 8.7 = 21 4

L<u>eBron - 2010</u>'s



27.1 PPG 2010's NBA: $\mu = 8.4$ ppg

27.1 – 8.4 = **18.7**





Paul Vathis, AP Images

Di

	30.1 PPG
	60's NBA: $\mu = 10.8 \text{ ppg}$
	30.1 - 10.8 =
iff:	19.3

30.1 PPG 90's NBA: μ = 8.7 ppg 30.1 – 8.7 = 21.4

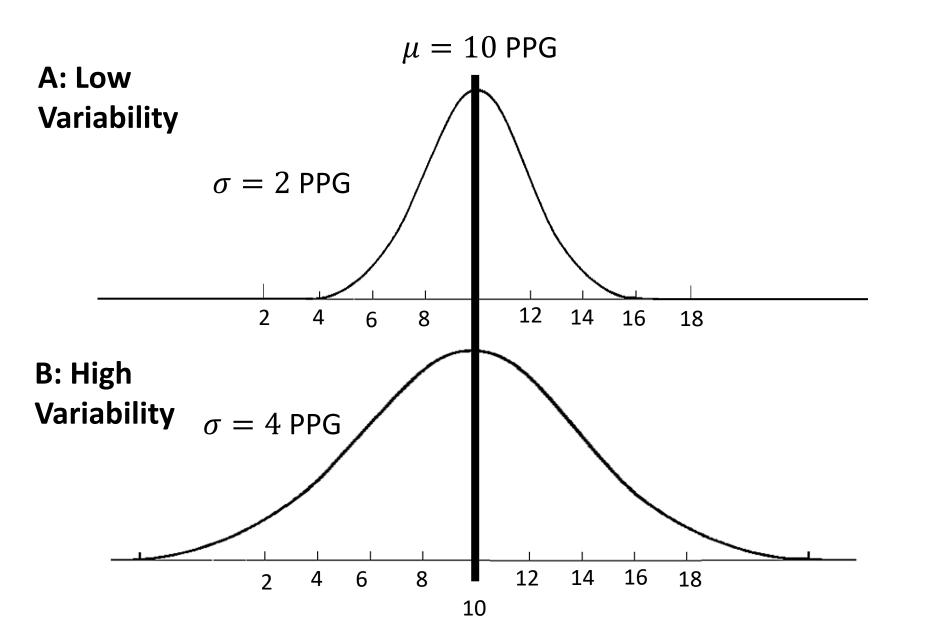
27.1 PPG 2010's NBA: $\mu = 8.4$ ppg 27.1 - 8.4 = 18.7

LeBron - 2010's

avaliers

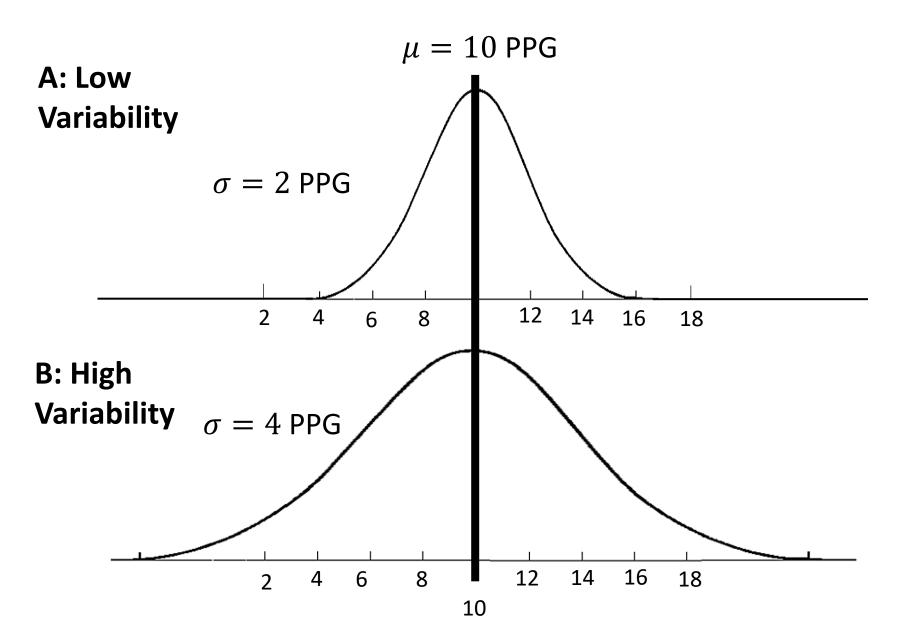
#3

Skew The Script



Skew The Script

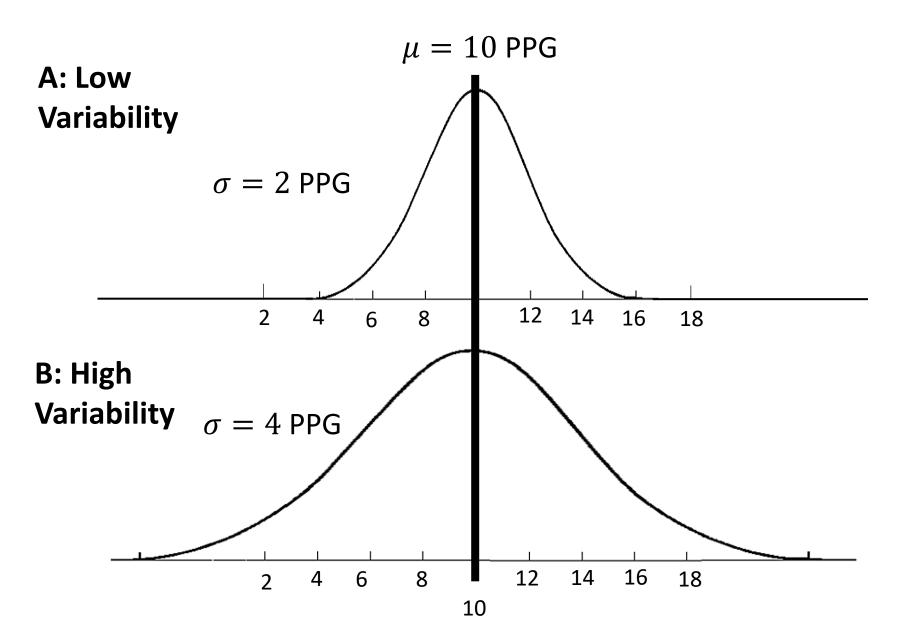
skewthescript.org





Skew The Script

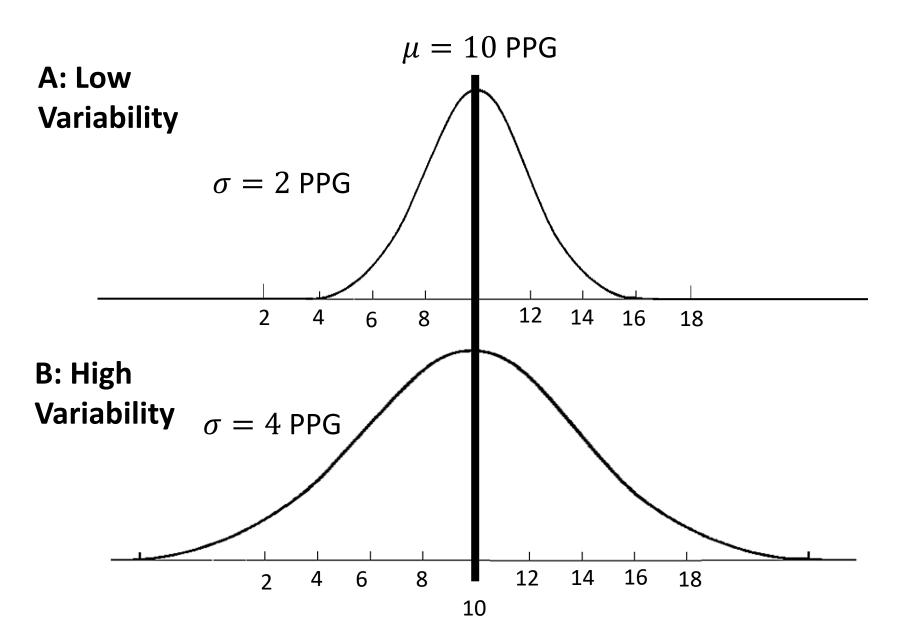
skewthescript.org





Skew The Script

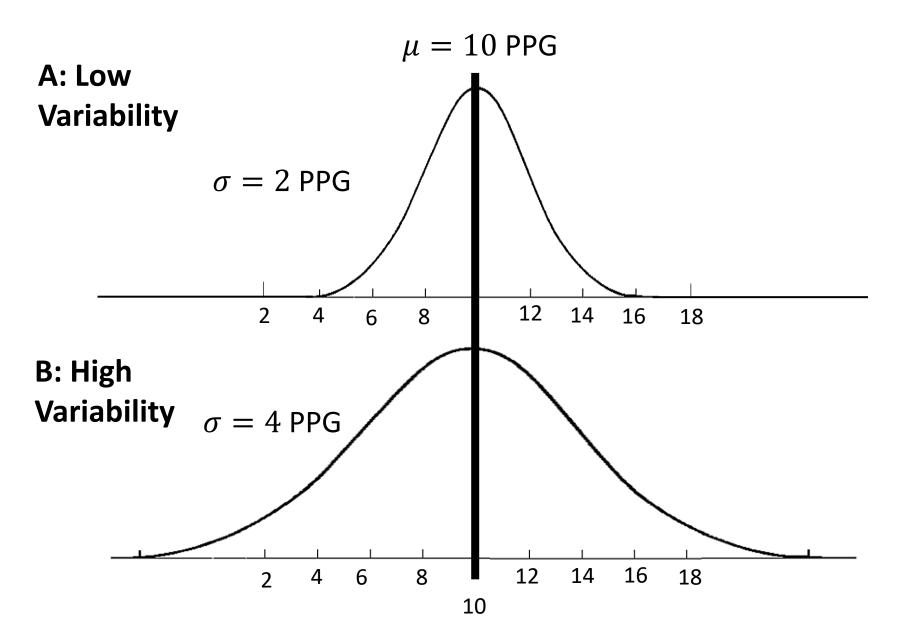
skewthescript.org





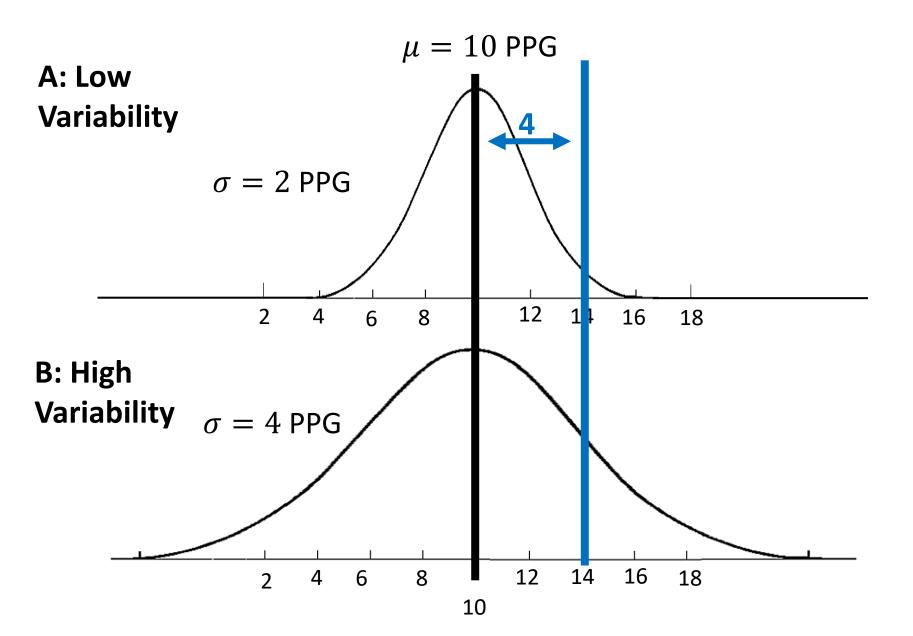
Skew The Script

skewthescript.org



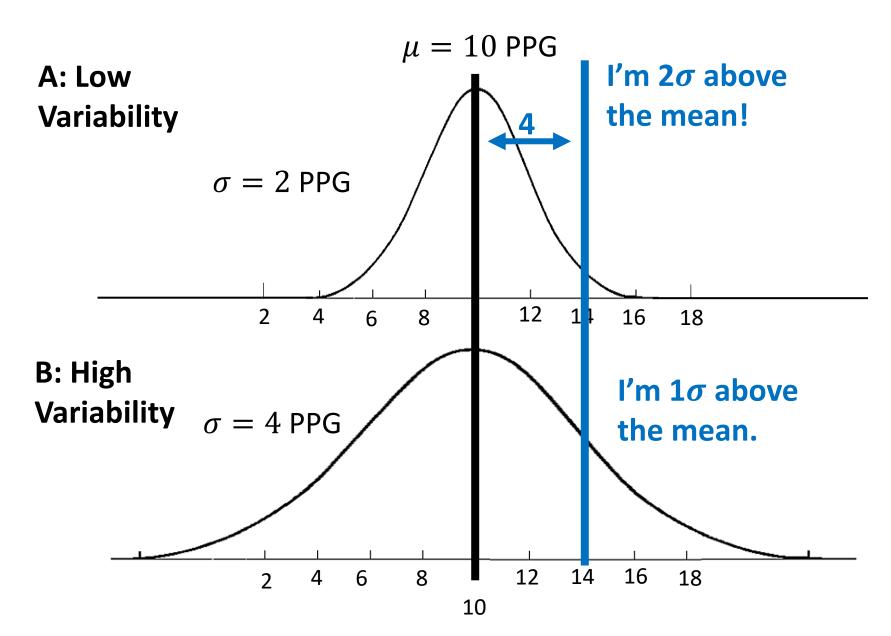






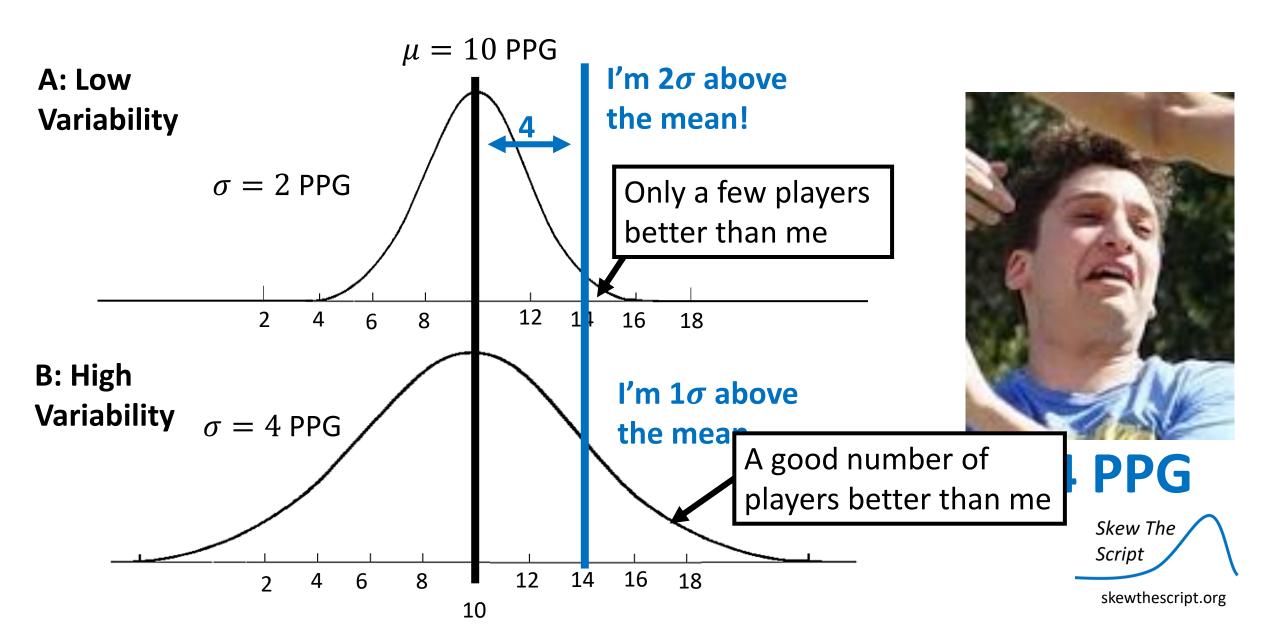








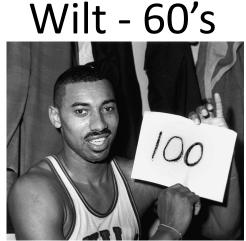




Standardization

A point's location in the distribution depends on **both** distance from the **center** and the distribution's **spread or variation**.





Paul Vathis, AP Images

Jordan - 90's



L<u>eBron - 2010</u>'s

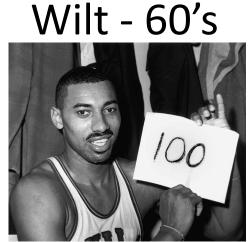


30.1 – 10.8 = <u>Diff:</u> **19.3** ppg

30.1 – 8.7 = **21.4** ppg

27.1 – 8.4 = **18.7** ppg





Paul Vathis, AP Images

30.1 - 10.8 = <u>Diff:</u> 19.3 ppg (σ) 7.0 ppg

Jordan - 90's



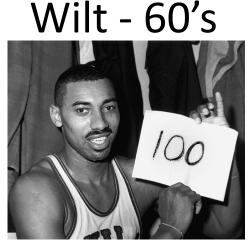
30.1 – 8.7 = 21.4 ppg 5.9 ppg

LeBron - 2010's



27.1 – 8.4 = **18.7** ppg **5.5** ppg





Paul Vathis, AP Images

(Z)

	30.1 - 10.8 =
Diff:	19.3 ppg
(σ)	7.0 ppg

Jordan - 90's



LeBron - 2010's



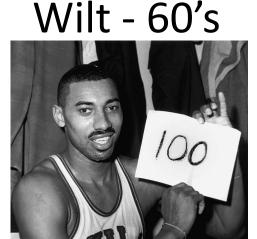
30.1 - 8.7 =**21.4** ppg **5.9** ppg

27.1 - 8.4 =**18.7** ppg **5.5** ppg



skewthescript.org

Z-score: The number of standard deviations away from the mean



Paul Vathis, AP Images

(Z)



<u>Jordan - 90's</u>



30.1 − 8.7 = **21.4** ppg **5.9** ppg

LeBron - 2010's

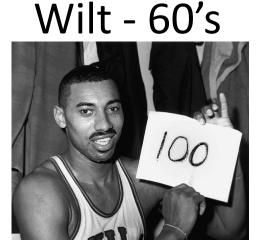


27.1 – 8.4 = **18.7** ppg **5.5** ppg

> Skew The Script

> > skewthescript.org

Z-score: The number of standard deviations away from the mean



30.1 - 10.8 =

19.3 ppg

2.8

7.0 ppg

Paul Vathis, AP Images

Diff:

(σ)

(Z)





30.1 – 8.7 = **21.4** ppg **5.9** ppg

3.6

LeBron - 2010's

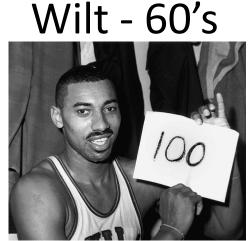


27.1 – 8.4 = **18.7** ppg **5.5** ppg

3.4



Z-score: The number of standard deviations away from the mean



Paul Vathis, AP Images

Jordan - 90's



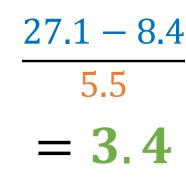
LeBron - 2010's



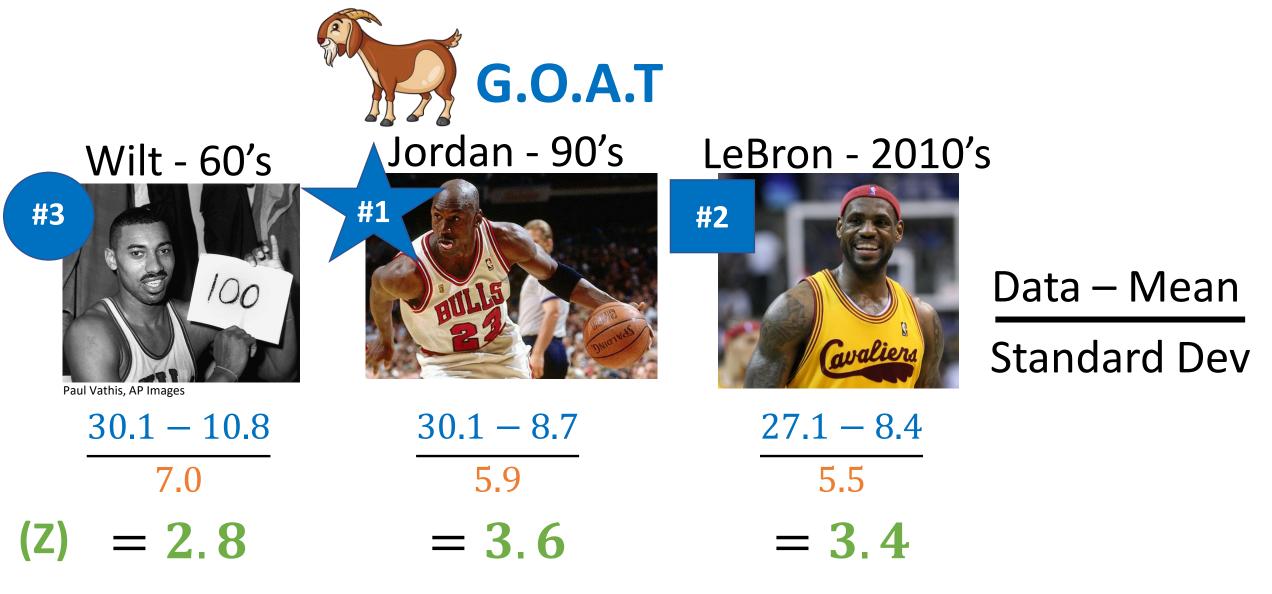
Data – Mean Standard Dev

	30.1 - 10.8			
	7.0			
(Z)	= 2.8			

30.1 - 8.7	
5.9	
= 3.6	









		G.O.A.T		
	Wilt - 60's	Jordan - 90's	L <u>eBron - 2010</u> '	S
#3 Pau	il Vathis, AP Images		#2	Data – Mean Standard Dev
	30.1 - 10.8	30.1 - 8.7	27.1 - 8.4	
	7.0	5.9	5.5	
(Z)	= 2.8	= 3.6	= 3.4	

MJ's PPG was **3.6** standard deviations **above** the mean for his era, making him the most **unusually high** scorer.





Adam Morrison, pictured where he spent most of his time with the Lakers: on the bench.

2009 Season: played 44 minutes **total**





Adam Morrison, pictured where he spent most of his time with the Lakers: on the bench.

2009 Season: played 44 minutes **total**



2,999 min



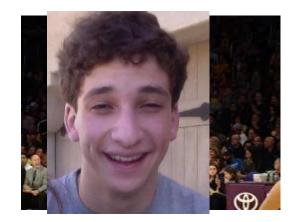
2,960 min

Skew The Script



Adam Morrison, pictured where he spent most of his time with the Lakers: on the bench.

2009 Season: played 44 minutes **total**



2,999 min



2,960 min

Skew The Script



Skew The Script















Skew The Script



Skew The Script



Skew The Script



Adam Morrison, pictured where he spent most of his time with the Lakers: on the bench.

While with the Lakers, he averaged **2.2 PPG**. (League: $\mu = 8.4$, $\sigma = 5.5$)





Adam Morrison, pictured where he spent most of his time with the Lakers: on the bench.

While with the Lakers, he averaged **2.2 PPG**. (League: $\mu = 8.4$, $\sigma = 5.5$)

$$z = \frac{data \ point - mean}{standard \ deviation}$$

Skew The Script



Adam Morrison, pictured where he spent most of his time with the Lakers: on the bench.

While with the Lakers, he averaged **2.2 PPG**. (League: $\mu = 8.4$, $\sigma = 5.5$)

$$z = \frac{data \ point - mean}{standard \ deviation}$$

$$z = \frac{2.2 - 8.4}{5.5}$$

Skew The Script



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Adam Morrison

Adam Morrison's scoring rate was 1.1 standard deviations **below** the league **average** in his era. While with the Lakers, he averaged **2.2 PPG**. (League: $\mu = 8.4$, $\sigma = 5.5$)

$$z = \frac{data \ point - mean}{standard \ deviation}$$

$$z = \frac{2.2 - 8.4}{5.5} = -1.1$$

Positive/Negative Z-Scores





2.2 PPG

27.1 PPG

z = 3.4

z = -1.1



Positive/Negative Z-Scores





2.2 PPG

27.1 PPG

z = -1.1

$$z = 3.4$$

 $z = \frac{data \ point - mean}{standard \ deviation}$

data > mean → positive data < mean → negative</p>

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Positive/Negative Z-Scores

Photo: opencourt-basketball.com

2.2 PPG



Positive Z-Score: The number of standard devs **above** the mean.

Negative Z-Score: The number of standard devs below the mean.

z = -1.1

Z =

data point – mean

standard deviation

z = 3.4

27.1 PPG

data > mean → positive data < mean → negative

Skew The Script



Pau Gasol



Kobe Bryant





Pau Gasol



Kobe Bryant







Pau Gasol



Kobe Bryant







Pau Gasol



Kobe Bryant



Adam Morrison





2010

Skew The Script



Adam Morrison





2009 2010

Skew The Script

skewthescript.org

has more championship rings than...



Adam Morrison



2009



2010

has more championship rings than...



Allen Iverson





Adam Morrison



2009



2010

has more championship rings than...



Russell Westbrook

Skew The Script



Adam Morrison



2009

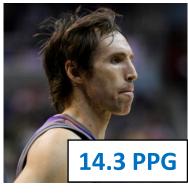


2010

has more championship rings than...







Steve Nash





Adam Morrison





2009

2010

has more championship rings than...

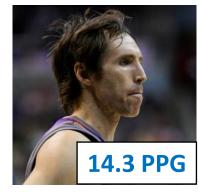


Allen Iverson



Russell Westbrook

23.2 PPG



Steve Nash

Skew The Script

skewthescript.org



Adam Morrison





2009

2010

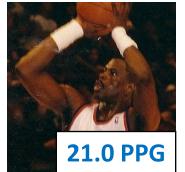
has more championship rings than...



Allen Iverson



Ewing



23.2 PPG

Russell Westbrook



Steve Nash

Skew The Script



Adam Morrison





2009

2010





Allen Iverson



Ewing











Steve Nash



Adam Morrison





2009

2010





Adam Morrison





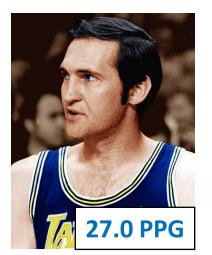
2009

2010





Adam Morrison



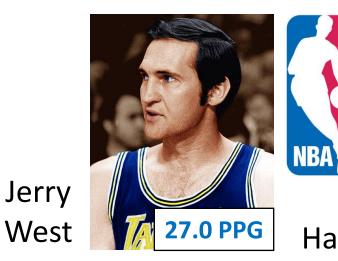
Jerry

West





Adam Morrison







Adam Morrison

has more championship rings than... **COMBINED**



Jerry West

It's all about the bling. G.O.A.T? has more championship rings than... COMBINED 2.2 PPG



Lesson 2.1 Discussion





Paul Vathis, AP Images

2.8 3.6 3.4 (Z)

• Jordan scored the most (relatively)

LeBron

avaliers





Paul Vathis, AP Images

2.8 3.6 3.4 (Z)

- Jordan scored the most (relatively)
- Is it because he shot the most?



Wilt

Jordan









Paul Vathis, AP Images

22.9 19.6 Shots per game



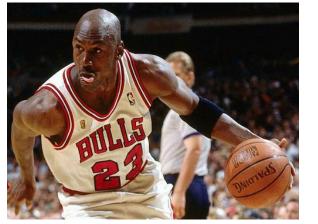
Wilt

Jordan





Paul Vathis, AP Images





22.5 22.9 19.6 Shots per game 54.0% 49.7% 50.4% % shots made







22.5	22.9	19.6	Shots per game
54.0%	49.7%	50.4%	% shots made

Discussion: Is Jordan still the G.O.A.T at scoring? What other stats may be helpful in determining who was the best?



Lesson 2.1 Practice

